

دانشگاه آزاد اسلامی واحد تبریز



نام درس: روش های رسمی در مهندسی نرم افزار

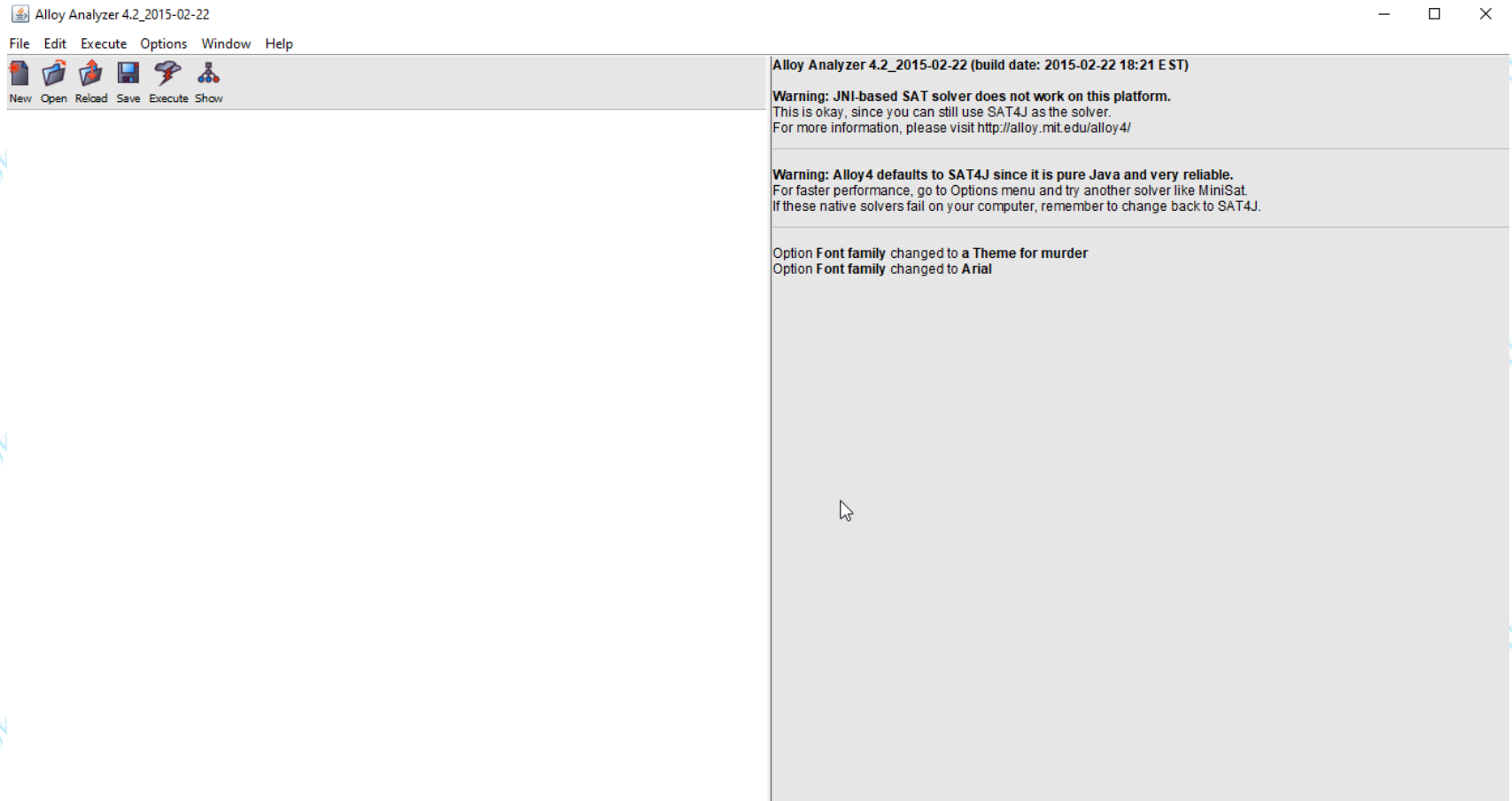
نخستین ابزار Alloy

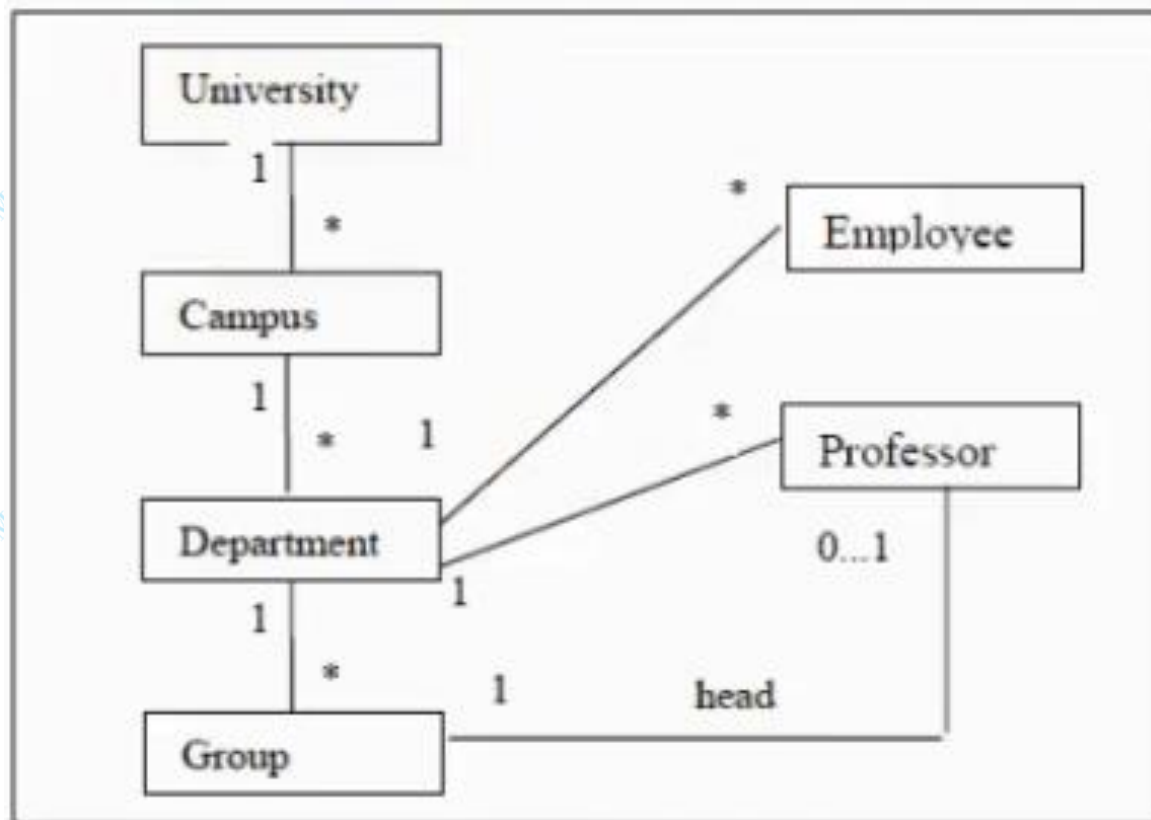
نام استاد: دکتر مسعود کارگر

Alloy tools

- Alloytools.org

Alloy tools





Example in alloy

```
module university
sig university{
  chairman:one professore,
  research: one professore,
  education: one professore
}
```

```
sig campus{
  belongsto:one university,
  chairman:one professore,
  research: one professore,
  education: one professore
}
```

```
sig department{
  chairman:one professore,
  research: one professore,
  education: one professore
}
```

```
sig group{
  head: one professore
}
```

```
sig professore{
  worksat: one group,
  member: one group
}
```

```
sig student {
  studiesat: one group
}
```

```
sig employee{
  worksat:one group
}
```

```
pred show(){}
run show
```

Abstract in model

```
module university
abstract sig educationalunit{
  chairman:one professore,
  research: one professore,
  education: one professore
}
```

```
sig university extends educationalunit {
}
```

```
sig campus extends educationalunit{
  belongsto:one university
}
```

```
sig department extends educationalunit{
}
```

```
sig group{
  head: one professore
}
```

```
sig professore{
  worksat: one group,
  member: one group
}
```

```
sig student {
  studiesat: one group
}
```

```
sig employee{
  worksat:one group
}
```

```
pred show(){}
run show
```

“Academia” Modeling Example

- We will model an academic enterprise expressing relationships between
 - People
 - Faculty
 - Students
 - Graduate
 - Undergraduate
 - Instructors – which can be grad students or faculty
 - Courses
 - Academic departments
 - Personal ID numbers

How should we model these basic domains in Alloy?

Strategy

- • Build and validate your model incrementally
 - Start with basic signatures and fields
 - Add basic constraints
 - Instantiate the model and study the results
 - Probe the model with assertions

Strategy

- • Add groups of features at a time
 - New signatures and fields
 - New constraints
 - Confirm previous assertions
 - Probe new features with assertions

Basic Components

- • People
 - Students: Undergrads and Grads
 - Instructors: Faculty and Grads
-
- Courses
 -
- Relationships
 - One instructor teaches a course
 - One or more students are taking a course
 - Students can be waiting for course

Academia Signatures

```
abstract sig Person {}  
sig Faculty extends Person {}  
abstract sig Student extends Person {}  
sig Graduate, Undergrad extends Student {}  
sig <Instructor in Person> {}  
  
sig Course {}  
...
```

We are not specifying here that instructors can only be graduate students or faculty. We will do that later with a "fact" constraint.

Academia Fields

- One instructor teaches a course
 - 2 choices:

```
sig Instructor in Person {  
  teaches: Course  
}
```

We cannot specify that there is exactly one instructor per course

```
fact oneInstrucPerCourse {  
  all c:Course | one teaches.c  
}
```

We have to add a fact specifying this constraint

```
sig Course {  
  taughtby: one Instructor }
```

Course Fields

- One instructor teaches a course
- One or more students are taking a course
- • Students can be waiting for course

Course Fields

- One instructor teaches a course
- One or more students are taking a course
- Students can be waiting for course

```
sig Course {
```

```
  taughtby: one Instructor,
```

```
  enrolled: some Student,
```

```
  waitlist: (set) Student
```

```
}
```

Exactly one instructor per course.

One or more students per course

Zero or more students per course

More relations

- We may choose to define auxiliary relations:

`teaches` (transpose of `taughtby`)

`taking` (transpose of `enrolled`)

`waitingfor` (transpose of `waitlist`)

`fun teaches: Instructor -> Course { ~taughtby }`

`fun taking: Student -> Course { ~enrolled }`

`fun waitingfor: Student -> Course { ~waitlist }`

- Or not:

if `i` is an instructor, then

`i.teaches <=> taughtby.i`

Note

- • Let i be an Instructor
- Let taughtby be the following binary relation
 - $\text{taughtby}: \text{Course} \rightarrow \text{one Instructor}$
- • The following expressions are equivalent and give a set of courses as result
 - $\text{taughtby}.i$
 - $i.\sim\text{taughtby}$
 - $i[\text{taughtby}]$

Academia Constraints

- All instructors are either faculty or graduate students

Was not expressed in set definition--although it could have, with

sig Instructor in Graduate + Faculty

- No one is waiting for a course unless someone is enrolled
- No graduate students teach a course that they are enrolled in

Academia Constraints

fact {

-- All instructors are either Faculty or Graduate Students

-- no one is waiting for a course unless someone is enrolled

-- (This is actually superfluous. Why?)

-- graduate students do not teach courses they are enrolled in
or waiting to enroll in

Academia Constraints

```
fact {
```

```
-- All instructors are either Faculty or Graduate Students
```

```
all i: Instructor | i in Faculty + Graduate
```

```
-- no one is waiting for a course unless someone is enrolled
```

```
-- (This is actually superfluous. Why?)
```

```
all c: Course |
```

```
    some c.waitlist => some c.enrolled
```

```
-- graduate students do not teach courses they are enrolled in  
or waiting to enroll in
```

```
all c: Course |
```

```
    c.taughtby !in c.enrolled + c.waitlist
```

Academia Realism Constraints

- There is a graduate student who is an instructor
- There are at least:
 - Two courses and
 - Three undergraduates

Academia Realism Constraints

Can be added to the model as facts, or just put in a run command to instruct the Alloy Analyzer to ignore unrealistic instances

```
pred RealismConstraints [] {  
  -- there is a graduate student who is an instructor  
  some Graduate & Instructor  
  
  -- there are at least two courses  
  #Course > 1  
  
  -- there are at least three undergraduates  
  #Undergrad > 2  
}
```

Academia Assertions

Let's check if our model has these properties:

- No instructor is on the waitlist for a course that he/she teaches
- No student is enrolled and on the waitlist for the same course

Academia Assertions

-- no instructor is on the waitlist for a course that he/she teaches

-- no student is enrolled and on the waitlist for the same course

Academia Assertions

-- no instructor is on the waitlist for a course that he/she teaches

```
assert NoWaitingTeacher {  
  all c: Course |  
    no (c.taughtby & c.waitlist)  
}
```

-- no student is enrolled and on the waitlist for the same course

```
assert NoEnrolledAndWaiting {  
  all c: Course |  
    no (c.enrolled & c.waitlist)  
}
```


Exercises

- Load academia-1.als
- With realism conditions enabled, do any instances exist in the default scopes?
 - Manipulate the scopes as necessary to obtain an instance under the realism conditions
- By looking at various sample instances, do you consider the model to be underconstrained in any way?
- Check assertions

Realism constraints

- • No instances exist in the default scope
-
- Why ?
-
- default scope:
at most 3 tuples in each top-level signature
-
- entails: at most 3 Students
-
- some Graduate & Instructor
#Undergrad > 2
-
- entails: at least 4 Students

Realism Constraints

```
pred [] RealismConstraints
{
  -- there is a graduate student who's an instructor
  some Graduate & Instructor

  -- there are at least two courses
  #Course > 1

  -- there are at least three undergraduates
  #Undergrad > 2
}
```

```
run RealismConstraints for 4
```

Instance

~~#Undergrad > 2~~ #Undergrad > 1

Instance found:

Signatures:

Course = {C0, C1}

Person = {U0, U1, G}

Faculty = {}

Student = {U0, U1, G}

Undergrad = {U0, U1}

Graduate = {G}

Instructor = {G}

Relations:

taughtby = { (C0, G), (C1, G) }

enrolled = { (C0, U1), (C1, U0) }

waitlist = { (C1, U1), (C1, U0) }

**Need to relate enrollment
and waiting lists**

Counter-example to assertion

Analyzing **NoEnrolledAndWaiting** ...

Counterexample found:

Signatures:

Course = {C}

Person = {G0, G1, F}

Faculty = {F}

Student = {G0, G1}

Undergrad = {}

Graduate = {G0, G1}

Instructor = {G0, G1}

Relations:

taughtby = { (C, G0) }

enrolled = { **(C, G1)** }

waitlist = { **(C, G1)** }

Academia Assertions

- No student is enrolled and on the waitlist for the same course
 - A counterexample has been found, hence we transform this assertion into a fact
- No instructor is on the waitlist for a course that he/she teaches
 - No counterexample

Academia Assertions

- NoWaitingTeacher assertion
 - No counterexample within the default scope
 - No counterexample within the scope 4, 5, 6, 10
- Can we conclude that the assertion is valid?
 - No! (It might have conterexamples but out of scope)
- But we take comfort in the
 - small scope hypothesis: if an assertion is not valid, it probably has a small counter-example

Why NoWaitingTeacher holds

- Assertion

- no instructor is on the waitlist for a course that he/she teaches

```
assert NoWaitingTeacher {  
  all c: Course | no (c.taughtby & c.waitlist)  
}
```

- Facts

- (i) faculty are not students and (ii) graduate students do not
 - teach courses they are enrolled in or waiting to enroll in

```
all c: Course |  
  c.taughtby !in c.enrolled + c.waitlist
```


Extension 1

- Add an attribute for students
 - Unique ID numbers
 - This requires a new signature
- Add student transcripts
- Add prerequisite structure for courses

New Relations

```
sig Id {}
```

```
abstract sig student extends Person {  
  id: one Id,  
  transcript: set Course  
}
```

```
sig Graduate, Undergrad extends student {}
```

```
sig Instructor in Person {}
```

```
sig Course {  
  taughtby: one Instructor,  
  enrolled: some Student,  
  waitlist: set Student,  
  prerequisites: set Course  
}
```

New Constraints

- Each Student is identified by one unique ID
 - Exactly one ID per Student
already enforced by multiplicities
 - No two distinct students have the same ID
has to be specified as a fact
- A student's transcript contains a course only if it contains the course's prerequisites
- A course does not have itself as a prerequisite
- Realism: there exists a course with prerequisites and with students enrolled

Academia Constraints

```
fact {  
  ...  
  -- A student's transcript contains a course only  
  -- if it contains the course's prerequisites  
  all s: Student |  
    s.transcript.prerequisites in s.transcript  
  
  -- A course does not have itself as a prerequisite  
all c: Course | c lin c.prerequisites not sufficient!  
}  
  
run {  
  ...  
  -- there is a course with prerequisites and  
  -- enrolled students  
  some c: Course |  
    some c.prerequisites and some c.enrolled  
}
```

Academia Constraints

```
fact {  
  ...  
  -- A student's transcript contains a course only  
  -- if it contains the course's prerequisites  
  all s: Student |  
    s.transcript.prerequisites in s.transcript  
  
  -- There are no cycles in the prerequisite dependencies  
  all c: Course | c !in c.^prerequisites  
}  
run {  
  ...  
  -- there is a course with prerequisites and  
  -- enrolled students  
  some c: Course |  
    some c.prerequisites and some c.enrolled  
}
```

Academia Assertions

- Students can only wait to be in a course for which they already have the prerequisites

```
assert AllwaitsHavePrereqs {  
  all s: student |  
    (waitlist.s).prerequisites in s.transcript  
}
```

Exercises

- • Load academia-2.als
-
- With realism conditions enabled, do any instances exist in the default scopes?
 - Manipulate the scopes as necessary to obtain an instance under the realism conditions
-
- By looking at various sample instances, do you consider the model to be underconstrained in any way?

Counter-example

Analyzing **AllWaitsHavePrereqs** ...

Counterexample found:

Signatures:

```
Id = {Id0, Id1, Id2}
Course = {C0, C1}
Person = {U, G0, G1}
Faculty = {}
Student = {U, G0, G1}
Undergrad = {U}
Graduate = {G0, G1}
Instructor = {G0, G1}
```

Relations:

```
taughtby = {(C0, G0), (C1, G0)}
enrolled = {(C0, U), (C1, G1)}
waitlist = {(C1, U)}
prerequisites = {(C1, C0)}
transcript = {(G1, C0)}
id = {(U, Id0), (G0, Id2), (G1, Id1)}
```

*U waits for the course C1
and
C0 is a prerequisite for C1
but
U does not have C0*

Where is (U, C0)?

New constraint

- • Old Assertion AllWaitsHavePrereqs
Students can wait only for those courses for which they already have the prerequisites
- • Old Fact
Students can have a course only if they already have the prerequisites
- • New Fact
Students can have, wait for or take a course only if they already have the prerequisites

New constraint

- New Fact: A student can have, wait for or take a course only if they already have the prerequisites

```
all s: Student |  
  (waitlist.s.prerequisites +  
   enrolled.s.prerequisites +  
   s.transcript.prerequisites)  
  in s.transcript
```

```
all s: Student |  
  (  
    waitlist.s + enrolled.s + s.transcript  
  ).prerequisites in s.transcript
```

Extension 2

- Add Departments, with
 - Instructors
 - Courses
 - Required courses
 - Student majors
- Add Faculty-Grad student relationships
 - Advisor
 - Thesis committee

Department Relations

- Each instructor is in a single department
 - Each department has at least one instructor
- Each department has some courses
 - Courses are in a single department
- Each student has a single department as his/her major

Faculty-Student Relations

- A *graduate* student has exactly one *faculty* member as an *advisor*
- *Faculty* members serve on *graduate* students' *committees*

New Relations

```
sig Faculty extends Person {  
  incommittee: set Graduate  
}
```

```
abstract sig Student extends  
Person {  
  major: one Department  
}
```

```
sig Graduate extends Student {  
  advisor: one Faculty  
}
```

```
sig Instructor in Person {  
  department:  
    one Department  
}
```

```
sig Department {  
  course: some Course,  
  required: some course  
}
```

Facts

-- Each department has at least one instructor

```
all d: Department | some department.d
```

-- Each course is in a single department

```
all c: Course | one course.c
```

New Constraints

- Advisors are on their advisees' committees
- Students are advised by faculty in their major
- Only faculty can teach required courses
- Faculty members only teach courses in their department
- Required courses for a major are a subset of the courses in that major
- Students must be enrolled in at least one course from their major

Exercise

- Express as an Alloy fact each of the new constraints in the previous slide

Advisors are on their advisees' committees

```
----- Signatures and Fields -----  
abstract sig Person {}  
sig Faculty extends Person {  
  incommittee: set Graduate  
}  
abstract sig student extends  
Person {  
  id: one Id,  
  transcript: set Course,  
  major: one Department  
}  
sig Undergrad extends Student {}  
sig Graduate extends Student {  
  advisor: one Faculty  
}  
sig Instructor in Person {  
  department: one Department  
}  
sig Course {  
  taughtby: one Instructor,  
  enrolled: some Student,  
  waitlist: set Student,  
  prerequisites: set Course  
}  
sig Id {}  
sig Department {  
  courses: some Course,  
  required: some Course  
}
```

Students are advised by faculty in their major

```
----- Signatures and Fields -----  
abstract sig Person {}  
sig Faculty extends Person {  
  incommittee: set Graduate  
}  
abstract sig student extends  
Person {  
  id: one Id,  
  transcript: set Course,  
  major: one Department  
}  
sig Undergrad extends student {}  
sig Graduate extends student {  
  advisor: one Faculty  
}  
sig Instructor in Person {  
  department: one Department  
}  
sig course {  
  taughtby: one Instructor,  
  enrolled: some student,  
  waitlist: set student,  
  prerequisites: set Course  
}  
sig Id {}  
sig Department {  
  courses: some Course,  
  required: some Course  
}
```

Required courses for a major are a subset of the courses in that major

----- Signatures and Fields -----

```
abstract sig Person {}  
sig Faculty extends Person {  
  incommittee: set Graduate  
}  
abstract sig Student extends  
Person {  
  id: one Id,  
  transcript: set Course,  
  major: one Department  
}  
sig Undergrad extends Student {}  
sig Graduate extends Student {  
  advisor: one Faculty  
}
```

```
sig Instructor in Person {  
  department: one Department  
}  
sig Course {  
  taughtby: one Instructor,  
  enrolled: some Student,  
  waitlist: set Student,  
  prerequisites: set Course  
}  
sig Id {}  
sig Department {  
  courses: some Course,  
  required: some Course  
}
```

Only faculty teach required courses

----- Signatures and Fields -----

```
abstract sig Person {}  
sig Faculty extends Person {  
  incommittee: set Graduate  
}  
abstract sig student extends  
Person {  
  id: one Id,  
  transcript: set Course,  
  major: one Department  
}  
sig Undergrad extends student {}  
sig Graduate extends student {  
  advisor: one Faculty  
}  
sig Instructor in Person {  
  department: one Department  
}  
sig Course {  
  taughtby: one Instructor,  
  enrolled: some Student,  
  waitlist: set student,  
  prerequisites: set Course  
}  
sig Id {}  
sig Department {  
  courses: some Course,  
  required: some Course  
}
```

Faculty members only teach courses in their department

```
----- Signatures and Fields -----  
abstract sig Person {}  
sig Faculty extends Person {  
  incommittee: set Graduate  
}  
abstract sig Student extends  
Person {  
  id: one Id,  
  transcript: set Course,  
  major: one Department  
}  
sig Undergrad extends Student {}  
sig Graduate extends Student {  
  advisor: one Faculty  
}  
sig Instructor in Person {  
  department: one Department  
}  
sig Course {  
  taughtby: one Instructor,  
  enrolled: some Student,  
  waitlist: set Student,  
  prerequisites: set Course  
}  
sig Id {}  
sig Department {  
  courses: some Course,  
  required: some Course  
}
```

Students must be enrolled in at least one course from their major

```
----- Signatures and Fields -----  
abstract sig Person {}  
sig Faculty extends Person {  
  incommittee: set Graduate  
}  
abstract sig student extends  
Person {  
  id: one Id,  
  transcript: set Course,  
  major: one Department  
}  
sig Undergrad extends student {}  
sig Graduate extends student {  
  advisor: one Faculty  
}  
sig Instructor in Person {  
  department: one Department  
}  
sig Course {  
  taughtby: one Instructor,  
  enrolled: some Student,  
  waitlist: set student,  
  prerequisites: set Course  
}  
sig Id {}  
sig Department {  
  courses: some Course,  
  required: some Course  
}
```

There are at least two departments and some required courses

----- Signatures and Fields -----

```
abstract sig Person {}
sig Faculty extends Person {
  incommittee: set Graduate
}
abstract sig Student extends
Person {
  id: one Id,
  transcript: set Course,
  major: one Department
}
sig Undergrad extends Student {}
sig Graduate extends Student {
  advisor: one Faculty
}

sig Instructor in Person {
  department: one Department
}
sig Course {
  taughtby: one Instructor,
  enrolled: some Student,
  waitlist: set Student,
  prerequisites: set Course
}
sig Id {}
sig Department {
  courses: some Course,
  required: some Course
}
```

A student's committee members are faculty in his/her major

----- Signatures and Fields -----

```
abstract sig Person {}  
sig Faculty extends Person {  
  incommittee: set Graduate  
}  
abstract sig Student extends  
Person {  
  id: one Id,  
  transcript: set Course,  
  major: one Department  
}  
sig Undergrad extends Student {}  
sig Graduate extends Student {  
  advisor: one Faculty  
}
```

```
sig Instructor in Person {  
  department: one Department  
}  
sig Course {  
  taughtby: one Instructor,  
  enrolled: some Student,  
  waitlist: set Student,  
  prerequisites: set Course  
}  
sig Id {}  
sig Department {  
  courses: some Course,  
  required: some Course  
}
```


Assertions

- Realism constraints: There are at least two departments and some required courses
- Assertion: A student's committee members are faculty in his/her major

Exercises

- Load academia-3.als
- With realism conditions enabled, do any instances exist in the default scopes?
- Manipulate the scopes as necessary to obtain an instance under the realism conditions
 - This requires some thought since constraints may interact in subtle ways
 - For example, adding a department requires at least one faculty member for that department
- Can you think of any more questions about the model?
 - Formulate them as assertions and see if the properties are already enforced by the constraints